

$$\begin{aligned} 45 &= 12(3) + 9 & 9 &= 45 - 12(3) \\ 12 &= 9(1) + 3 & 3 &= 12 - 9(1) \\ 9 &= 3(3) + 0 \end{aligned}$$

$$\begin{aligned} 3 &= 12 - 9(1) \\ &= 12 - (45 - 12(3))(1) \\ &= 12 - 45 + 12(3) \\ &= 12(4) + 45(-1) \end{aligned}$$

$$\begin{aligned} 45 &= 12(3) + 9 & 9 &= 45 + 12(-3) \\ 12 &= 9(1) + 3 & 3 &= 12 + 9(-1) \\ 9 &= 3(3) + 0 \end{aligned}$$

$$\begin{aligned} 3 &= 12 - 9(1) \\ &= 12 - \frac{(45 + 12(-3))(1)}{45 + 12(3)} \\ &= 12(4) + 45(-1) \end{aligned}$$

$$\begin{array}{l} 245 = 90(2) + 65 \\ 90 = 65(1) + 25 \\ 65 = 25(2) + 15 \\ 25 = 15(1) + 10 \\ 15 = 10(1) + 5 \\ 10 = 5(2) + 0 \end{array} \quad \begin{array}{l} 65 = 245 + 90(-2) \\ 25 = 90 + 65(-1) \\ 15 = 65 + 25(-2) \\ 10 = 25 + 15(-1) \\ 5 = 15 + 10(-1) \end{array}$$

$$\begin{aligned} 5 &= 15 + 10(-1) \\ &= 15 + \frac{(25 + 15(-1))(-1)}{25(-1) + 15(1)} \\ &= 15(2) + 25(-1) \\ &= \frac{(65 + 25(-2))(2)}{65(2) + 25(-4)} + 25(-1) \\ &= 65(2) + 25(-5) \\ &= 65(2) + \frac{(90 + 65(-1))(-5)}{90(-5) + 65(5)} \\ &= 65(7) + 90(-5) \\ &= \frac{(245 + 90(-2))(7)}{245(7) + 90(-14)} + 90(-5) \\ &= 245(7) + 90(-19) \end{aligned}$$

**The target to gather together is always a prior remainder. Substitution is in reverse order of above right equations.**